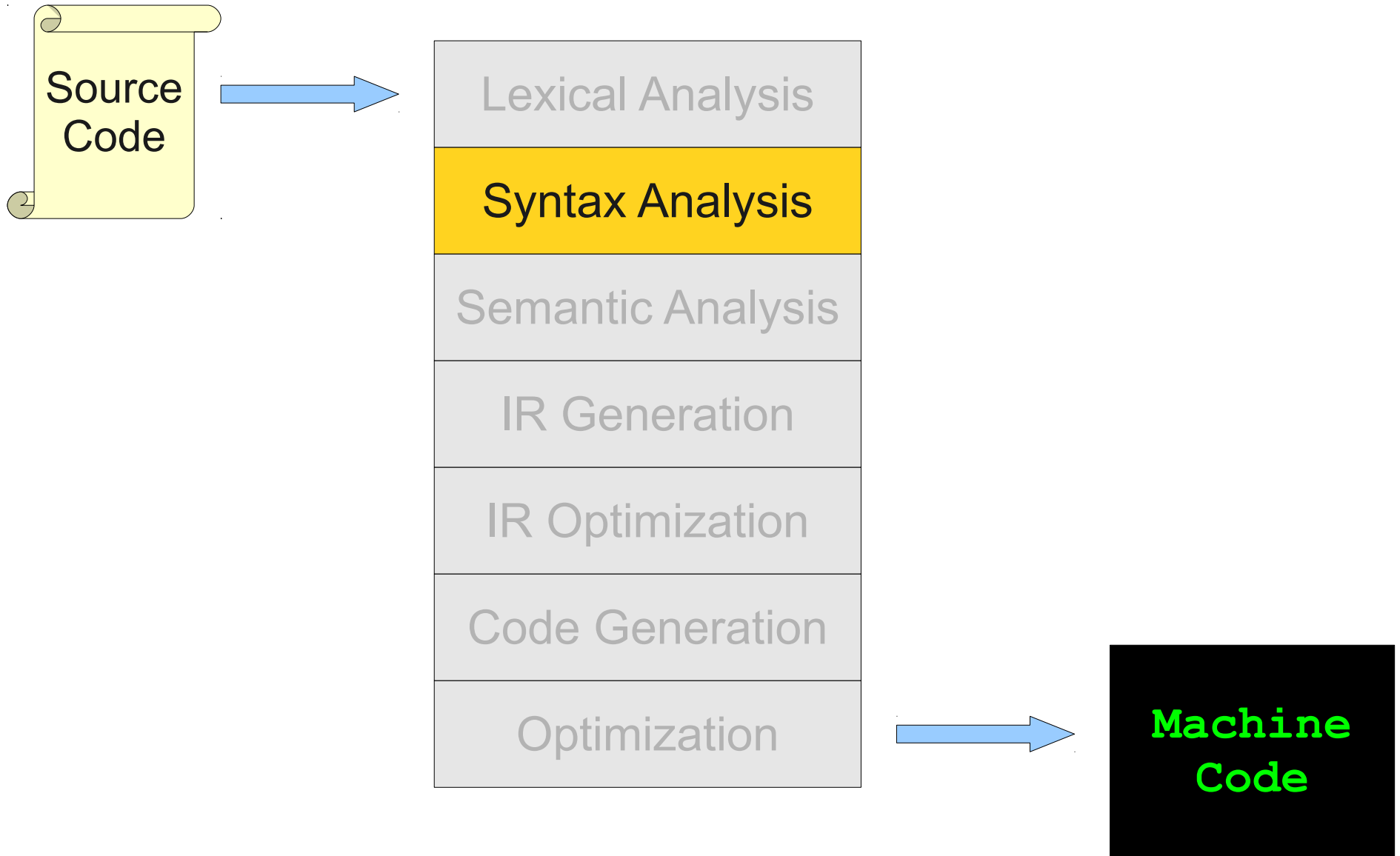


Top-Down Parsing, Part II

Announcements

- Programming Project 1 due **Friday, 11:59PM**
- Office hours every day until then.
- Submission instructions will be emailed out tonight.

Where We Are



Review of LL(1)

- Left-to-right scan, Leftmost derivation, 1 token lookahead.
- Predict which production to use based on the current nonterminal and the lookahead token.
- Build an **LL(1) parse table** to make these lookups fast and streamlined.

Review of FIRST Sets

- The set **FIRST(A)** is defined as the set of terminals that could be at the start of a string ultimately derived from A.
 - Formally: $\text{FIRST}(A) = \{ t \mid A \rightarrow^* tv \}$
- Can compute iteratively:
 - Set $\text{FIRST}(A) = \{ t \mid A \rightarrow tv \}$
 - Keep computing $\text{FIRST}(A) = \text{FIRST}(A) \cup \text{FIRST}(B)$ for all productions $A \rightarrow wBv$, where w is a string of nonterminals that can derive ϵ .

Review of FOLLOW Sets

- The set **FOLLOW(A)** is defined as the set of terminals that could potentially follow a string produced from nonterminal A.
- Formally: $\text{FOLLOW}(A) = \{ t \mid B \rightarrow^* uAtv \}$
- Can also be computed iteratively:
 - Initially, set $\text{FOLLOW}(A) = \text{FIRST}(w) - \{\epsilon\}$ for all rules $C \rightarrow vAw$.
 - Keep computing $\text{FOLLOW}(A) = \text{FOLLOW}(A) \cup \text{FOLLOW}(B)$ for all rules $B \rightarrow vAw$ where w is or can derive ϵ .

LL(1) Table Construction

- Compute $\text{FIRST}(A)$ and $\text{FOLLOW}(A)$ for all nonterminals A .
- For each rule $A \rightarrow w$ and for each **terminal** t in $\text{FIRST}(w)$, set $T[A, t] = w$.
 - Note that ϵ is **not** a terminal!
- For each rule $A \rightarrow w$ with ϵ in $\text{FIRST}(w)$, set $T[A, t] = w$ for each t in $\text{FOLLOW}(A)$.

Example LL(1) Construction

The Limits of LL(1)

A Grammar that is Not LL(1)

- Consider the following (left-recursive) grammar:

$$A \rightarrow Ab \mid c$$

- $\text{FIRST}(A) = \{c\}$
- However, we cannot build an LL(1) parse table.
- **Why?**

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- **Why?**

	b	c
A		$A \rightarrow Ab$ $A \rightarrow c$

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- **Why?**

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- **Cannot uniquely predict production!**
- This is called a **FIRST/FIRST** conflict.

Eliminating Left Recursion

- In general, left recursion can be converted into **right recursion** by a mechanical transformation.

- Consider the grammar

$$A \rightarrow Av \mid w$$

- This will produce w followed by some number of v 's.
- Can rewrite the grammar as

$$A \rightarrow wB$$

$$B \rightarrow \varepsilon \mid vB$$

Another Non-LL(1) Grammar

- Consider the following grammar:

$S \rightarrow E$

$E \rightarrow T$

$E \rightarrow T + E$

$T \rightarrow \mathbf{int}$

$T \rightarrow (E)$

- $\text{FIRST}(E) = \{ \mathbf{int}, (\}$
- $\text{FIRST}(T) = \{ \mathbf{int}, (\}$
- Why is this grammar not LL(1)?

Another Non-LL(1) Grammar

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- $\text{FIRST}(T) = \{ \text{int}, (\}$
- Why is this grammar not LL(1)?

How do you
predict which of
these to use?

Left-Factoring

$S \rightarrow E$

$E \rightarrow T$

$E \rightarrow T + E$

$T \rightarrow \text{int}$

$T \rightarrow (E)$

Left-Factoring

$$S \rightarrow E$$
$$E \rightarrow T\epsilon$$
$$E \rightarrow T + E$$
$$T \rightarrow \mathbf{int}$$
$$T \rightarrow (E)$$

Left-Factoring

$S \rightarrow E$

$E \rightarrow T\epsilon$

$E \rightarrow T + E$

$T \rightarrow \mathbf{int}$

$T \rightarrow (E)$

$Y \rightarrow + E$

$Y \rightarrow \epsilon$

Left-Factoring

$S \rightarrow E$

$E \rightarrow TY$

$T \rightarrow \mathbf{int}$

$T \rightarrow (E)$

$Y \rightarrow + E$

$Y \rightarrow \varepsilon$

Left-Factoring

$S \rightarrow E$

$E \rightarrow TY$

$T \rightarrow \text{int}$

$T \rightarrow (E)$

$Y \rightarrow + E$

$Y \rightarrow \varepsilon$

	int	()	+	\$
S					
E					
T					
Y					

Left-Factoring

$S \rightarrow E$

$E \rightarrow TY$

$T \rightarrow \text{int}$

$T \rightarrow (E)$

$Y \rightarrow + E$

$Y \rightarrow \varepsilon$

FIRST			
S	E	T	Y

	int	()	+	\$
S					
E					
T					
Y					

Left-Factoring

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$E \rightarrow TY$

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FIRST			
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int (int (int (+ ϵ
FOLLOW			
S	E	T	Y
\$	\$)		

	int	()	+	\$
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FIRST			
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int (int (int (+ ϵ
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FIRST			
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int (int (int (+ ϵ
FOLLOW			
S	E	T	Y
\$	\$)	+ \$)	\$)

	int	()	+	\$
S					
E					
T					
Y					

Left-Factoring

$S \rightarrow E$	1
$E \rightarrow TY$	2
$T \rightarrow \text{int}$	3
$T \rightarrow (E)$	4
$Y \rightarrow + E$	5
$Y \rightarrow \epsilon$	6

FIRST			
S	E	T	Y
int	int	int	+
(((ϵ
FOLLOW			
S	E	T	Y
\$	\$	+	\$
)	\$)
)	

	int	()	+	\$
S					
E					
T					
Y					

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FIRST			
S	E	T	Y
int (int (int (+ ϵ
FOLLOW			
S	E	T	Y
\$	\$)	+ \$)	\$)

	int	()	+	\$
S	1	1			
E					
T					
Y					

Left-Factoring

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FIRST			
S	E	T	Y
int	int	int	+
(((ϵ
FOLLOW			
S	E	T	Y
\$	\$	+	\$
)	\$)
)	

	int	()	+	\$
S	1	1			
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	int	()	+	\$
S	1	1			
E	2	2			
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FOLLOW			
S	E	T	Y
\$	\$	+	\$
)	\$)
)	

	int	()	+	\$
S	1	1			
E	2	2			
T	3	4			
Y			6	5	6

The Strengths of LL(1)

LL(1) is Realistic

- Some real-world programming languages are LL(1)-parsable or parsable with a minor modification on LL(1).
- Examples:
 - LISP
 - Python
 - JavaScript

LL(1) is Straightforward

- Can be implemented quickly with a table-driven design.
- Can be implemented by **recursive descent**:
 - Define a function for each nonterminal.
 - Have these functions call each other based on the lookahead token.
- See Handout #09 for more details.

LL(1) is Fast

- Both table-driven LL(1) and recursive-descent-powered LL(1) are fast.
- Can parse in $O(n f(G))$ time, where n is the length of the string and $f(G)$ is some function of the size of the grammar (usually a small constant).

Summary

- **Top-down parsing** tries to derive the user's program from the start symbol.
- **Leftmost BFS** is one approach to top-down parsing; it is mostly of theoretical interest.
- **Leftmost DFS** is another approach to top-down parsing that is uncommon in practice.
- **LL(1)** parsing scans from left-to-right, using one token of lookahead to find a leftmost derivation.
- **FIRST sets** contain terminals that may be the first symbol of a production.
- **FOLLOW sets** contain terminals that may follow a nonterminal in a production.
- **Left recursion** and **left factoring** cause LL(1) to fail and can be mechanically eliminated.